Consider the equation for the trajectory of a particle along a circle of radius $r$ centered at $(a, b)$:

$$
(x_t - a)^2 + (y_t - b)^2 = r^2. \tag{1}
$$

There are three unknowns: $a$, $b$, and $r$. To compute these unknowns from the path, we need two more equations. Let’s differentiate (and divide by 2):

$$
(x_t - a)\dot{x}_t + (y_t - b)\dot{y}_t = 0. \tag{2}
$$

And one more time:

$$
(x_t - a)\ddot{x}_t + (y_t - b)\ddot{y}_t + \dot{x}_t^2 + \dot{y}_t^2 = 0. \tag{3}
$$

We want to solve for the three unknowns in terms of the values and derivatives of the trajectory at time $t$. First, we solve (2) for $y_t - b$ in terms of $x_t - a$:

$$
y_t - b = -(x_t - a)\frac{\dot{x}_t}{\dot{y}_t}. \tag{4}
$$

Next, we substitute this formula into (1) and solve for $x_t - a$:

$$
x_t - a = \frac{r}{\sqrt{1 + (\dot{x}_t/\dot{y}_t)^2}} = \frac{\dot{y}_t r}{\sqrt{\dot{x}_t^2 + \dot{y}_t^2}}.
$$

From this, we see that

$$
y_t - b = -\frac{\dot{x}_t r}{\sqrt{\dot{x}_t^2 + \dot{y}_t^2}}. \tag{5}
$$

We then plug these formulas for $x_t - a$ and $y_t - b$ into (3) to get an equation involving only unknown $r$:

$$
\frac{\dot{y}_t r \ddot{x}_t}{\sqrt{\dot{x}_t^2 + \dot{y}_t^2}} - \frac{\dot{x}_t r \ddot{y}_t}{\sqrt{\dot{x}_t^2 + \dot{y}_t^2}} + \dot{x}_t^2 + \dot{y}_t^2 = 0.
$$

Solving for $r$ and squaring both sides, we get

$$
r^2 = \frac{(\dot{x}_t^2 + \dot{y}_t^2)^3}{(\dot{y}_t \dot{x}_t - \dot{x}_t \dot{y}_t)^2}.
$$